

Math 150 Test 1
Name: Key
Show all necessary steps Clearly, Neatly, and Systematically to receive full credit. Any Incorrect statement will be penalized.

1. Find the equation of the line passes through the points $\left(1, \frac{1}{2}\right)$ and $\left(2, \frac{1}{3}\right)$. Write the result in standard form.

$$\begin{aligned}
 m &= \frac{y_2 - y_1}{x_2 - x_1} & y - y_1 &= m(x - x_1) \\
 &= \frac{\frac{1}{3} - \frac{1}{2}}{2 - 1} & y - \frac{1}{2} &= -\frac{1}{6}(x - 1) \\
 &= \frac{-\frac{1}{6}}{1} & y - \frac{1}{2} &= -\frac{1}{6}x + \frac{1}{6} \\
 &= -\frac{1}{6} & \frac{1}{6}x + y - \frac{1}{2} &= \frac{1}{6} \\
 & & \frac{1}{6}x + y &= \frac{1}{6} + \frac{1}{2} \\
 & & \frac{1}{6}x + y &= \frac{4}{6} \\
 & & \frac{1}{6}x + y &= \frac{2}{3} // \quad \cong \quad x + 6y = 4 //
 \end{aligned}$$

2. Solve: $\frac{x-1}{6} + x = \frac{2}{3} - \frac{x+2}{6}$

$$6 \left(\frac{x-1}{6} + x \right) = 6 \left(\frac{2}{3} - \frac{x+2}{6} \right)$$

$$1(x-1) + 6x = 4 - 1(x+2)$$

$$x - 1 + 6x = 4 - x - 2$$

$$7x - 1 = -x + 2$$

$$8x - 1 = 2$$

$$8x = 3$$

$$x = \frac{3}{8}$$

$$\left\{ \frac{3}{8} \right\} //$$

3. A pile of sand is in the shape of a cone whose radius is 10 feet and whose height is 6 feet. Find the amount of sand in the pile.

$$\text{Area} = 10 \quad V = \left(\frac{1}{3}\right) \pi r^2 h$$
$$h = 6$$
$$V = ?$$
$$= \frac{1}{3} \cdot \pi \cdot (10)^2 \cdot (6)$$
$$= 200\pi \text{ ft}^3 //$$

4. Solve: $I = a + (n-1)d$. for n .

$$I - a = (n-1)d$$

$$\frac{I - a}{d} = n - 1$$

$$\frac{I - a}{d} + 1 = n //$$

or

$$\frac{I}{d} - \frac{a}{d} + 1 = n //$$

5. Simplify: $10 \left[\frac{3}{5}(2s+2t) - \frac{5}{4}(s-t) + 1 \right]$

$$= 10 \left[\frac{6}{5}s + \frac{6}{5}t - \frac{5}{4}s + \frac{5}{4}t + 1 \right]$$

$$= 10 \left[-\frac{1}{20}s + \frac{49}{20}t + 1 \right]$$

$$= -\frac{1}{2}s + \frac{49}{2}t + 10 //$$

side

$$\frac{6}{5} - \frac{5}{4}$$

$$\frac{24}{20} - \frac{25}{20}$$

$$\frac{6}{5} + \frac{5}{4}$$

$$\frac{24}{20} + \frac{25}{20}$$

6. Solve: $6 - (x-3) - 5x = 3[1 - 2(x+2)]$.

$$6 - x + 3 - 5x = 3[1 - 2x - 4]$$

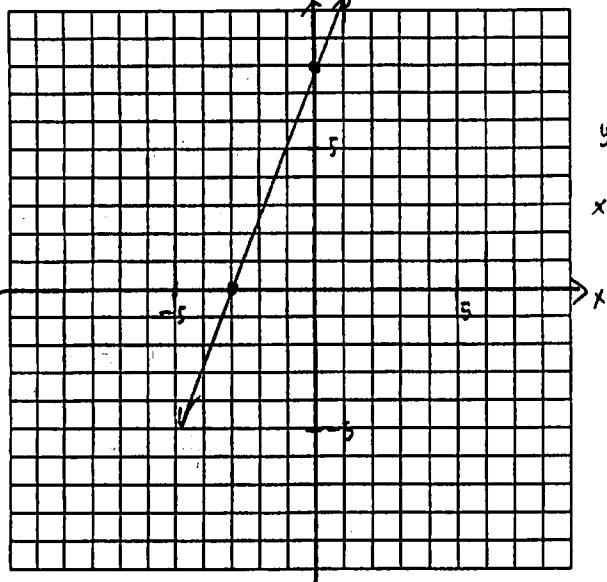
$$-6x + 9 = 3[-2x - 3]$$

$$-6x + 9 = -6x - 9$$

$$9 = -9 \leftarrow \text{false}$$

∅

7. Find x-intercept and y-intercept of the line: $\frac{2}{3}x - \frac{1}{4}y = -2$. Then graph.



	x	y
y-intercept	0	8
x-intercept	-3	0

$$\begin{aligned}\frac{2}{3}(0) - \frac{1}{4}y &= -2 & \frac{2}{3}x - \frac{1}{4}(0) &= -2 \\ -\frac{1}{4}y &= -2 & \frac{2}{3}x &= -2 \\ y &= 8 & x &= -3\end{aligned}$$

8. A large warehouse stores 150 more computers than printers. The monthly storage cost for a computer is \$2.50 and a printer is \$1.50. If storage for the computers and printers is \$2775 per month, how many printers and computers are in the warehouse? (make sure to show in 3-step format)

$$\# \text{ of computers} = x + 150$$

$$\# \text{ of printers} = x$$

$$2.50(x + 150) + 1.50(x) = 2775$$

$$2.5x + 375 + 1.5x = 2775$$

$$4x + 375 = 2775$$

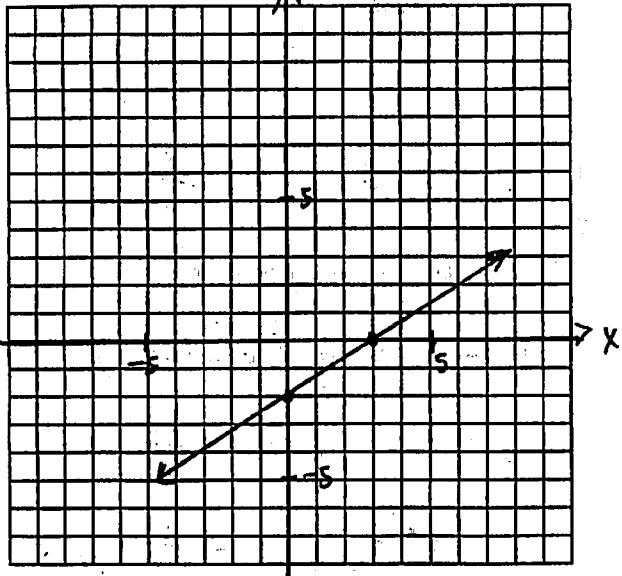
$$4x = 2400$$

$$x = 600$$

<u>y</u>	<u>side</u>
3	150
+	25
<hr/>	
7	50
+	3000
<hr/>	
3	750

There are 1750 computers and 600 printers.

9. Find the slope and y-intercept of the line: $0.4x - 0.6y = 1.2$. Then graph.



$$10. (0.4x - 0.6y) = (1.2) \cdot 10$$

$$4x - 6y = 12$$

$$-6y = -4x + 12$$

$$y = \frac{-4x + 12}{-6}$$

$$y = \frac{2}{3}x - 2$$

$$m = \frac{2}{3}$$

$$\text{y-intercept} = (0, -2)$$

10. The measure of one angle is 15° less than half of the other angle. Find the measure of each angle if they are supplementary. (make sure to show in 3-step format)

$$\text{measure of one angle} = \frac{1}{2}x - 15$$

$$\text{measure of other angle} = x$$

$$(\frac{1}{2}x - 15) + x = 180$$

$$\frac{3}{2}x - 15 = 180$$

$$\frac{3}{2}x = 195$$

$$x = 130$$

$$\begin{array}{r} \underline{\text{side}} \\ \underline{65} \\ 195 \cdot \frac{2}{3} \end{array}$$

measure of other angle is 130° and measure of one angle is 50°

11. Find the equation of the line which passes through the point $(-2, 3)$ and parallel to the line $-4x + 6y + 10 = 0$. Write the result in slope-intercept form.

$$\underline{\underline{d_2}} \quad -4x + 6y + 10 = 0$$

$$6y = 4x - 10$$

$$y = \frac{4}{6}x - \frac{10}{6}$$

$$y = \frac{2}{3}x - \frac{5}{3}$$

$$m = \frac{2}{3}$$

$$\underline{\underline{l_1}} \quad (-2, 3), m = \frac{2}{3}$$

$$y - y_1 = m(x - x_1)$$

$$y - 3 = \frac{2}{3}(x - (-2))$$

$$y - 3 = \frac{2}{3}x + \frac{4}{3}$$

$$y = \frac{2}{3}x + \frac{13}{3} //$$

side

$$\frac{4}{3} + \frac{3}{1}$$

$$\frac{4}{3} + \frac{9}{3}$$

12. A 186-foot television cable is to be cut into four pieces. Find the length of each piece if each successive piece is 3 feet longer than the previous one. (make sure to show in 3-step format)

$$\text{length of } 1^{\text{st}} \text{ piece.} = x$$

$$\text{II } 2^{\text{nd}} \text{ " } = x + 3$$

$$\text{III } 3^{\text{rd}} \text{ " } = x + 6$$

$$\text{IV } 4^{\text{th}} \text{ " } = x + 9$$

$$x + (x+3) + (x+6) + (x+9) = 186$$

$$4x + 18 = 186$$

$$4x = 168$$

$$x = 42$$

$$\text{length of } 1^{\text{st}} \text{ piece} = 42 \text{ ft}$$

$$\text{II } 2^{\text{nd}} \text{ " } = 45 \text{ ft}$$

$$\text{III } 3^{\text{rd}} \text{ " } = 48 \text{ ft}$$

$$\text{IV } 4^{\text{th}} \text{ " } = 51 \text{ ft}$$