

Math 150

Test 4

Name: _____

Show all necessary steps Clearly, Neatly, and Systematically to receive full credit. Any incorrect statement will be penalized.

1. (6) Solve: $\sqrt{-k+2} + 2 = k$

$$\sqrt{-k+2} = k - 2$$

$$(\sqrt{-k+2})^2 = (k-2)^2$$

$$-k+2 = k^2 - 4k + 4$$

$$0 = k^2 - 3k + 2$$

$$0 = (k-2)(k-1)$$

$$k-2 = 0 \quad k-1 = 0$$

$$k = 2 \quad k = 1$$

$$\{ 2 \}$$

2. (6) Simplify: $\left(w^{\frac{2}{3}}x^{-\frac{1}{2}}\right)^{-2} \left(2w^{-\frac{3}{4}}x^{-\frac{5}{8}}\right)^{-6}$

$$= w^{-\frac{4}{3}} x^{-6} w^{\frac{9}{2}} x^{\frac{15}{4}}$$

$$= \frac{1}{2^6} w^{-\frac{4}{3} + \frac{9}{2}} x^{1 + \frac{15}{4}}$$

$$= \frac{1}{64} w^{-\frac{19}{6}} x^{-\frac{19}{4}}$$

$$= \frac{1}{64} w^{-\frac{19}{6}} x^{-\frac{19}{4}}$$

3. (6) Simplify:

a. $\frac{5}{4i}$

$$= \frac{5}{4i} \cdot \frac{i}{i}$$

$$= \frac{5i}{4i^2}$$

$$= \frac{5}{-4} i //$$

b. $(\sqrt{121} + \sqrt{-169})(\sqrt{225} - \sqrt{-289})$

$$= (11 + 13i)(15 - 17i)$$

$$= 165 - 187i + 195i - 221i^2$$

$$= 165 + 8i + 221$$

$$= 386 + 8i //$$

4. (6) It takes one team 9 days less than another to survey 1000 people. If the teams work together, it takes them 20 days to complete such a survey. How long will it take each to do the survey alone?

	w	t	= wc
team 1	$\frac{1}{x-9}$	$x-9$	1
team 2	$\frac{1}{x}$	x	1

$$\left(\frac{1}{x-9} + \frac{1}{x} \right) \cdot 20 = 1$$

$$x - 45 = 0 \quad x - 4 = 0 \\ x = 45 \quad x \neq 4$$

$$\frac{20}{x-9} + \frac{20}{x} = 1$$

$$x(x-9) \left(\frac{20}{x-9} + \frac{20}{x} \right) = 1 \cdot x \cdot (x-9)$$

$$20x + 20(x-9) = x^2 - 9x$$

$$20x + 20x - 180 = x^2 - 9x$$

$$0 = x^2 - 49x + 180$$

$$0 = (x-45)(x-4) \nearrow$$

team 1 takes 36 days and
team 2 takes 45 days //

5. (6) Simplify:

a. $x^3\sqrt{-48x^4y^6} - x^2y^3\sqrt{-162xy^3} + 7\sqrt[3]{6x^7y^6}$

$$\begin{aligned} &= x \cdot (-2x^2y^2)\sqrt[3]{6x} - x^2y \cdot (-3y)\sqrt[3]{6x} + 7 \cdot (x^2y^2)\sqrt[3]{6x} \\ &= -2x^2y^2\sqrt[3]{6x} + 3x^2y^2\sqrt[3]{6x} + 7x^2y^2\sqrt[3]{6x} \\ &= 8x^2y^2\sqrt[3]{6x} // \end{aligned}$$

b. $\sqrt{4\sqrt{6\sqrt{8\sqrt{x^{10}}}}}$

$$\begin{aligned} &= (((x^{\frac{10}{8}})^{\frac{1}{2}})^{\frac{1}{4}})^{\frac{1}{2}} \\ &= x^{\frac{5}{192}} // \end{aligned}$$

6. (6) The intensity of light received from a light source varies inversely as the square of the distance from the light source. If a photographer, 16 feet away from his subject, has a light meter reading of 4 foot-candles of luminance, what will the meter read if the photographer moves in for a close-up 2 feet away from the subject. (make sure define all the variables and set up formula)

I = intensity of light

d = distance.

$$I = \frac{k}{d^2} \rightarrow I = \frac{1024}{d^2}$$

$$4 = \frac{k}{16^2} \quad I = \frac{1024}{(16)^2}$$

$$4 = \frac{k}{256} \quad I = 256 //$$

$$1024 = k$$

7. (6) Solve: $(a^2 + 6a)^{\frac{1}{4}} = 2(a-1)^{\frac{1}{4}}$

$$\sqrt[4]{a^2 + 6a} = 2 \sqrt[4]{a-1}$$

$$(\sqrt[4]{a^2 + 6a})^4 = (2 \sqrt[4]{a-1})^4$$

$$a^2 + 6a = 16(a-1)$$

$$a^2 + 6a = 16a - 16$$

$$a^2 - 10a + 16 = 0$$

$$(a-8)(a-2) = 0 \quad \{ 8, 2 \}$$

$$a-8=0 \quad a-2=0$$

$$a=8 \quad a=2$$

8. (6) Solve: $(10-\sqrt{t})^2 - 4(10-\sqrt{t}) - 45 = 0$.

Let $u = 10 - \sqrt{t}$

$$u^2 - 4u - 45 = 0$$

$$(u-9)(u+5) = 0$$

$$u-9=0 \quad u+5=0$$

$$10 - \sqrt{t} - 9 = 0 \quad 10 - \sqrt{t} + 5 = 0$$

$$1 - \sqrt{t} = 0 \quad 15 - \sqrt{t} = 0$$

$$1 = \sqrt{t} \quad 15 = \sqrt{t}$$

$$1 = t \quad 225 = t$$

$$\{ 1, 225 \}$$

9. (6) Rationalize the denominator: $\frac{2\sqrt{x}-3\sqrt{y}}{\sqrt{4x+9y}}$

$$= \frac{2\sqrt{x}-3\sqrt{y}}{2\sqrt{x}+3\sqrt{y}} \cdot \frac{2\sqrt{x}-3\sqrt{y}}{2\sqrt{x}-3\sqrt{y}}$$

$$= \frac{4x - 12\sqrt{xy} + 9y}{4x - 9y}$$

10. (6) Solve: $\sqrt{x+16} + \sqrt{x+9} = 7$

$$\sqrt{x+16} = 7 - \sqrt{x+9}$$

$$(\sqrt{x+16})^2 = (7 - \sqrt{x+9})^2$$

$$x+16 = 49 - 14\sqrt{x+9} + x+9$$

$$x+16 = 58 + x - 14\sqrt{x+9}$$

$$-42 = -14\sqrt{x+9}$$

$$3 = \sqrt{x+9}$$

$$(3)^2 = (\sqrt{x+9})^2$$

$$9 = x+9$$

$$0 = x$$

11. (6) Simplify: $\frac{\sqrt{36} - \sqrt{-49}}{\sqrt{64} + \sqrt{-81}}$

$$= \frac{6 - 7i}{8 + 9i}$$

$$= \frac{6 - 7i}{8 + 9i} \cdot \frac{8 - 9i}{8 - 9i}$$

$$= \frac{48 - 54i - 56i + 63i^2}{64 - 81i^2}$$

$$= \frac{-15 - 110i}{64 + 81}$$

$$= -\frac{3}{29} - \frac{22}{29}i //$$

$$= -\frac{15}{145} - \frac{110}{145}i$$

12. (6) In a scale drawing, a 280-foot antenna tower is drawn $7\frac{1}{2}$ inches high. The building next to it is drawn $2\frac{1}{4}$ inches high. How tall is the actual building?

building let x = height of actual building.
pic

$$\frac{280}{7\frac{1}{2}} = \frac{x}{2\frac{1}{4}}$$

$$\frac{280}{\frac{15}{2}} = \frac{x}{\frac{9}{4}}$$

$$280 \cdot \frac{9}{4} = \frac{15}{2}x$$

$$x = 84$$

$$630 = \frac{15}{2}x$$

the building is 84 ft tall.

$$630 \cdot \frac{2}{15} = x$$

13. (6) Solve by completing the square method: $4m^2 + 2m + 3 = 0$

$$4m^2 + 2m = -3$$

$$m^2 + \frac{1}{2}m = -\frac{3}{4}$$

$$m^2 + \frac{1}{2}m + \frac{1}{16} = -\frac{3}{4} + \frac{1}{16}$$

$$(m + \frac{1}{4})^2 = -\frac{11}{16}$$

$$m + \frac{1}{4} = \pm \sqrt{-\frac{11}{16}}$$

$$m + \frac{1}{4} = \pm \frac{\sqrt{11}}{4} i$$

$$m = -\frac{1}{4} \pm \frac{\sqrt{11}}{4} i //$$

14. (6) Solve: $x^{\frac{2}{3}} + 6x^{\frac{1}{3}} = 16$

$$\text{Let } u = x^{\frac{1}{3}} = \sqrt[3]{x}$$

$$u^2 + 6u = 16$$

$$u^2 + 6u - 16 = 0$$

$$(u+8)(u-2) = 0$$

$$u+8=0 \quad u-2=0$$

$$\sqrt[3]{x} + 8 = 0 \quad \sqrt[3]{x} - 2 = 0$$

$$\sqrt[3]{x} = -8 \quad \sqrt[3]{x} = 2$$

$$x = (-8)^3 \quad x = (2)^3$$

$$x = -512 \quad x = 8$$

$$\{-512, 8\} //$$

15. (3,4) Let the equation be $-x^2 = \frac{7x+1}{5}$. $\rightarrow -5x^2 = 7x + 1 \rightarrow 0 = 5x^2 + 7x + 1$

a. Use the discriminant to determine the number and type of solutions.

$$b^2 - 4ac = (7)^2 - 4(5)(1)$$

$$= 49 - 20$$

$$= 29$$

2 real irrational solutions //

b. Use the quadratic formula to solve the equation.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-7 \pm \sqrt{29}}{2(5)}$$

$$= \frac{-7 \pm \sqrt{29}}{10} //$$

16. (6) Solve: $3(2-y)^2 + 7 = 32$

$$3(2-y)^2 = 25$$

$$(2-y)^2 = \frac{25}{3}$$

$$2-y = \pm \sqrt{\frac{25}{3}}$$

$$2-y = \pm \frac{5}{\sqrt{3}}$$

$$2-y = \pm \frac{5\sqrt{3}}{3}$$

$$-y = -2 \pm \frac{5\sqrt{3}}{3}$$

$$y = 2 \pm \frac{5\sqrt{3}}{3} //$$